### **Abstract**

*Linear Algebra*, my undergraduate text, has long been freely available online.

I recently adapted it for paper. I will discuss some differences in delivering work in the two formats that current authors can apply, and some things about today's landscape of print on demand.

# Moving an Online Book to Paper

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Lon Mitchell, 13c@orthogonalpublishing.com

TEX Users Group, 2014-July

## Linear Algebra

- ▶ Available for download since 1996-ish, with 上下 source.
- Standard US sophmore course, for students who are not future PhD's, necessarily.
- 497 pages, with extensive question sets, worked answers for every question, and with classroom beamer slides and a lab manual.
- Under the GNU Free Documentation License or the Creative Commons CC BY-SA license (for Wikibooks).

## Linear Algebra

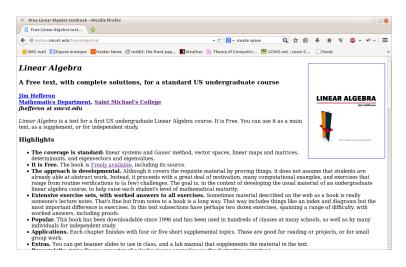
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In part because of its early start, and perhaps because of some merit, it is on the first page of a Google search for "linear algebra."

I get 30K-40K downloads per week (I have seen a million but that may have been some script run amok).

## Until recently how you got it

In 1996 I spent a lot of time online reading about how the future is online. I decided to distribute via downloads.



### The model

In the past how it worked is that an instructor printed the PDF, copied that, put it in a comb binding, and students paid what it took to defray the cost. Thus, students had copies of copies.

- Page size is US letter, 8.5 x 11 inches.
- In 1996 printers were 300 dpi. Some shading and graphics vanished, or did Morié effects.
- Computer Modern characters had dropouts so I went to the Concrete font with Euler for math.
- Instructors might omit printing parts such as the Preface, the Bibliography, or some optional material.
- Colors in the PDF became gray when printed. You can't be ambitious with color.

### Desire for other versions, from users ...

Sometimes self-studiers ask for physical copies.

Send me a copy at this address .... You didn't say how much a copy costs. Enclosed is a check for \$50. If that is not enough put a note in the envelope and I'll send you more.

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Sometimes potential adopters tell me that they did not use it because it requires them to have it printed. (Even at my home college, having the printshop cart copies directly to the bookstore nearly got both managers fired.)

## ... from entrepeneurs ...

From: XXXXXXXXXXX

Sent: Tuesday, April 01, 2014 21:33

To: Hefferon, James S.

Subject: [\*\*Possible SCAM email\*\*] Love your textbook work

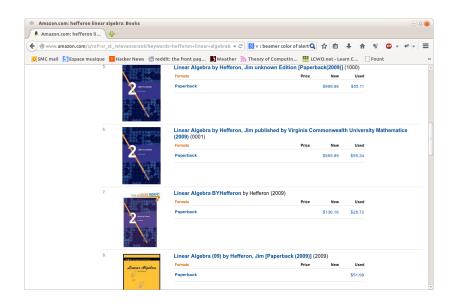
Mr. Hefferon,

My name is XXXXXXX, and I'm the CEO/cofounder of a startup called XXXXXXXX(http://www.XXXXX.com), we provide a platform for textbook writers and publishers to publish their books over the web.

I found a link to your textbook at this website: http://www.randomhacks.net/articles/2007/03/07/hefferon-linear-algebra-review, and I gotta say: I think your work is impressive!

All our books are published via both the web, print, and mobile devices. We also are pioneering an open-publication system, where anyone can suggests errata via version control/pull requests, so that you remain in control whether you want to accept the changes or not. Our users own their book for life, so they immediately receive all updates, making our texts, in a way, become living (i.e. the books never really expire, and quality tends to increase over time with each revision). All of our books are accessible to people with disabilities (blind, and dyslexic). We also spend a lot of time researching usability patterns to make our books as easy to read as possible. Our system also utilizes a lot of different systems to make every text searchable. We take every highlight done using our system as a signal indicating which parts of the text are most important, thus creating a highlight heat map of the text.

# ... and from those who push the entrepeneurial envelope



### A note from Lon Mitchell



My first semesters using your book were marred, however, by student reviews ... students commented that they did not like using untested and unproven course material – they did not like being "guinea pigs."

... I also noticed that many students, for whatever reason, refused to print out a copy to have in class. I'm still at a loss to explain this phenomenon: why will students sacrifice potential educational benefits for \$10-\$15 when they are paying so much more in tuition?

... Studies have shown that many students, even up to 75%, still prefer a print edition to an electronic textbook. Studies have also shown that many students forgo purchasing a required textbook to try and save money.

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# He proposes to go down the rabbit hole, to paper

My project to produce a print version of your text was to try and reply to these concerns. In particular, I wanted a book that would look professional enough that students would not have a reason to believe it was anything less than professional quality (or at least the quality of other linear algebra books). I also wanted something they could find in the bookstore.

He started a low-profit company, an L3C, to look for more open-source books to help into print. (If you are interested, write him at l3c@orthogonalpublishing.com.)

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# I'm pretty innocent at this



## From the selfpub.net FAQ

### How do I get my book listed on Amazon.com and BarnesandNoble.com?

- ...You will want your book to be listed in the Ingram distribution channel. When Amazon or Barnes and Noble wants to purchase a book they first look to Ingram who carries millions of book titles in their inventory.
- ... If the retailer does not have the title in stock they will request a copy from Ingram. If Ingram does not have a copy in stock the order will be sent to your print-on-demand printer who will print and likely drop-ship the book to the customer. You just sit back and collect your check for your percentage of the sales made.

Two popular print-on-demand companies who distribute to Ingram are:

- Lightning Source which is owned by Ingram and offers print-on-demand book printing for self-publishing authors and small press publishers.
- CreateSpace which is part of Amazon. They offer two services for distribution. The first option lists your book for sale on Amazon.com. With their expanded distribution, your book will be distributed through Ingram and made available to all retailers.

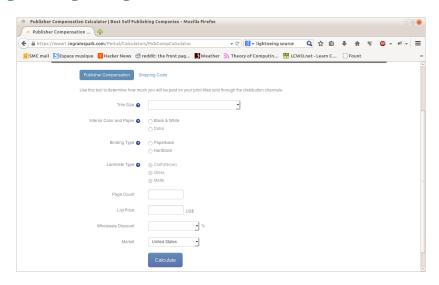
# Who to choose? The big two



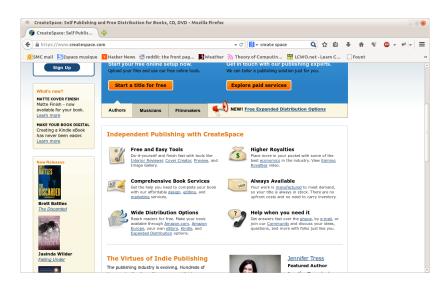
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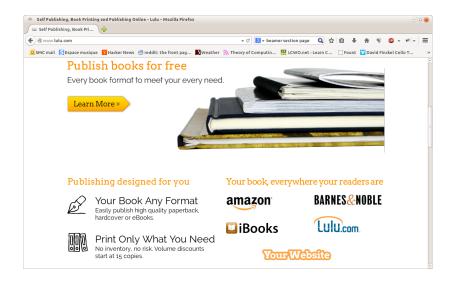
# Ingram (Lightning Source)



### **Amazon**



### There are others: Lulu



### Into the dark

It may well be that Amazon is so powerful now that having a book only for sale there is enough, and students will certainly be able to find it that way. Amazon seems to have a good reputation for some things, including ease of author use and customer service. If someone wants to work on their own then that may be the best way.

### Into the dark

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However, the deal may come with strings.



For instance, you can offer an ebook as free to read on the Kindle for two weeks but you have to agree to exclusivity with Amazon.

#### Revenue

We tell retailers what price to charge buyers. They deduct a certain percentage, the *discount*, and then give the rest to us, for the printing and for profit.

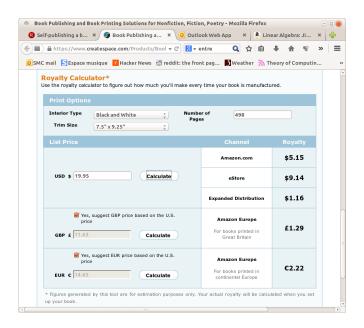
#### Revenue

We tell retailers what price to charge buyers. They deduct a certain percentage, the *discount*, and then give the rest to us, for the printing and for profit.

The odd part is that we get to set an upper limit on the retailer's percentage. The bricks and mortar standard is 55%. If we set the percentage too low then these retailers will not offer the book. But online retailers are fine with 25% (college bookstores also accept this low percentage) so I went with this.

Amazon's Createspace or Lulu don't have a discount because you are already working with the retailer. The downside is that you may have restricted distribution, or face a double mark-up such as Lulu books that are sold on Amazon.

### Amazon's calculator



## Printing costs

Printing prices are significantly less for certain book sizes. US paper size  $8.5 \times 11$  inches is expensive. Cheaper are  $6 \times 9$ ,  $6.14 \times 9.21$ ,  $6.69 \times 9.61$ ,  $7.5 \times 9.25$ , and  $7.44 \times 9.69$ .

The  $6.14 \times 9.21$  size is common for upper-level textbooks. The smaller width means more reformatting, however, and lower-level textbooks are often larger, so I went with  $7.5 \times 9.25$ . Besides, this size retains the option for an instructor to print the text onto  $8.5 \times 11$ .

### Additional considerations

Our other costs are setup fees (\$105), ISBNs (\$25 each), and an annual listing fee (\$13).

ISBN costs are a downside to frequent updates, as traditionally any major or even many minor changes in a book should result in a new edition with a new ISBN (the disadvantage is clear of students purchasing editions with the same ISBN that are significantly different).

Having a little extra revenue from each copy helps with things like advertising, such as free books for the Joint Math Meeting.

Finally, with a Free book anyone could undercut the price. However most people go to my web page for the book and I point to my edition.

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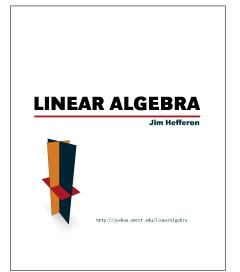
The takeaway: We used Lightning Source at a \$20 list price, which splits about into thirds for printing, for the retailer, and for Lon and I.

### Cover

- ► The cover is one file, with front, back, and spine. If a revision adds or removes pages then the size of the spine changes so you want to create the cover using a process that can be easily redone (I arranged it all in 上下上 picture environment).
- There is no printing on the inside of the cover. My driver .tex file got a flag so that if the PDF is for paper then it makes an extra inside sheet holding the page with the list of symbols. (This flag also makes hyperlinks in the book's body show as black instead of the electronic PDF's blue.)
- My 498 pages gives a spine width of 1.001 inches.
- ➤ The back cover has some marketing text. The ISBN and bar code go at the bottom of the back, in a box about an inch tall.

### Cover art

I have no artistic ability, at all. I seem also to have no ability to get others to use *their* artistic ability.



### Binding energy

The 7.5 x 9.25 inche book size allows me to keep  $\&T_EX$ 's default line length of 345 points and printing onto US 8.5 x 11 paper is not too bad.

The more pages there are, the more the binding will use up page space, so the inside margins needed to be set a little larger.

Repaginating the mathematics took longer than you would think. The microtype package helps with linebreaks, and using \raggedbottom and forbidding widows and orphans helps with pagebreaks, but neither help nearly enough.

#### Lurking culprits

At the first submission, besides the binding margin there was only one thing to fix: a non-embedded type 3 font somewhere in the document. Using XPDF's pdffonts showed that it was on pages 295 and 296. The only unusual things to see there was graphs from *Sage*.

Some spelunking<sup>1</sup> revealed that I needed to pass to the Sage plot the parameter typeset=latex. That bug ticket was only a couple of months old.

<sup>1</sup>http://trac.sagemath.org/ticket/14664

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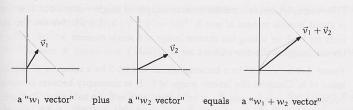
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## There's 0.85 gray and then there's 0.70 gray

2.8 Example A homomorphism can express an analogy between spaces that is more subtle than the prior one. For the map from Example 2.6

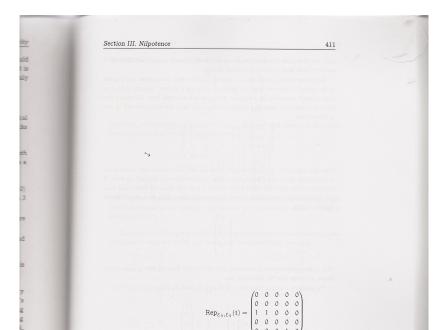
$$\begin{pmatrix} x \\ y \end{pmatrix} \xrightarrow{h} x + y$$

fix two numbers in the range  $w_1,w_2\in\mathbb{R}$ . A  $\vec{v}_1$  that maps to  $w_1$  has components that add to  $w_1$ , so the inverse image  $h^{-1}(w_1)$  is the set of vectors with endpoint on the diagonal line  $x+y=w_1$ . Think of these as " $w_1$  vectors." Similarly we have " $w_2$  vectors" and " $w_1+w_2$  vectors." The addition preservation property says this.



Restated, if we add a  $w_1$  vector to a  $w_2$  vector then h maps the result to a  $w_1 + w_2$  vector. Briefly, the sum of the images is the image of the sum. Even more briefly,  $h(\vec{v}_1) + h(\vec{v}_2) = h(\vec{v}_1 + \vec{v}_2)$ .

# Mistakes look *really* bad in print



for numbers m1, ..., mk that measure the quantities.

For the second fact, observe that an easy way to construct a dimensionally homogeneous expression is by taking a product of dimensionless quantities or by adding such dimensionless terms. Buckingham's Theorem states that any complete relationship among quantities with dimensional formulas can be algebraically manipulated into a form where there is some function f such that

$$f(\Pi_1, ..., \Pi_n) = 0$$

for a complete set  $\{\Pi_1,\ldots,\Pi_n\}$  of dimensionless products. (The first example below describes what makes a set of dimensionless products 'complete'.) We usually want to express one of the quantities,  $m_1$  for instance, in terms of the others. For that we will assume that the above equality can be rewritten

$$m_1 = m_2^{-p_2} \cdots m_k^{-p_k} \cdot \hat{f}(\Pi_2, \dots, \Pi_n)$$

where  $\Pi_1 = m_1 m_1^{p_2} \cdots m_t^{p_s}$  is dimensionless and the products  $\Pi_2, \ldots, \Pi_n$  don't involve  $m_1$  (as with f, here  $\hat{f}$  is an arbitrary function, this time of n-1 arguments). Thus, to do dimensional analysis we should find which dimensionless products are possible.

For example, again consider the formula for a pendulum's period.

BACKSON STREET	quantity	formula
	period p	L <sup>0</sup> M <sup>0</sup> T <sup>1</sup>
	length of string ℓ	L <sup>1</sup> M <sup>0</sup> T <sup>0</sup>
1	mass of bob m	L <sup>0</sup> M <sup>1</sup> T <sup>0</sup>
0	acceleration due to gravity q	L1M0T-2
	arc of swing $\theta$	L <sup>o</sup> M <sup>o</sup> T <sup>o</sup>

- 1.15 The proof of Lemma 1.5 contains a reference to the  $\mathfrak{i}\neq\mathfrak{j}$  condition on the row combination operation.
  - (a) Write down a 2×2 matrix with nonzero entries, and show that the -1 · ρ<sub>1</sub> + ρ<sub>1</sub> operation is not reversed by 1 · ρ<sub>1</sub> + ρ<sub>1</sub>.
  - (b) Expand the proof of that lemma to make explicit exactly where it uses the  $i \neq j$  condition on combining.
- 1.16 [Cleary] Consider the set of students in a class. Which of the following relationships are equivalence relations? Explain each answer in at least a sentence.
  - (a) Two students x, y are related if x has taken at least as many math classes as y.(b) Students x, y are related if they have names that start with the same letter.
- 1.17 Show that each of these is an equivalence on the set of  $2\times 2$  matrices. Describe
- the equivalence classes.

  (a) Two matrices are related if they have the same product down the diagonal,
  - that is, if the product of the entries in the upper left and lower right are equal.
    (b) Two matrices are related if they both have at least one entry that is a 1, or if neither does.
- 1.18 Show that each is not an equivalence on the set of 2×2 matrices.
  - (a) Two matrices A, B are related if α<sub>1,1</sub> = -b<sub>1,1</sub>.
  - (b) Two matrices are related if the sum of their entries are within 5, that is, A is related to B if  $|(\alpha_{1,1}+\cdots+\alpha_{2,2})-(b_{1,1}+\cdots+b_{2,2})|<5$ .

#### III.2 The Linear Combination Lemma

We will close this chapter by proving that every matrix is row equivalent to one and only one reduced echelon form matrix. The ideas here will reappear, and be further developed, in the next chapter.

The crucial observation concerns how row operations act to transform one

### Typical chapter page

Chapter Two

### **Vector Spaces**

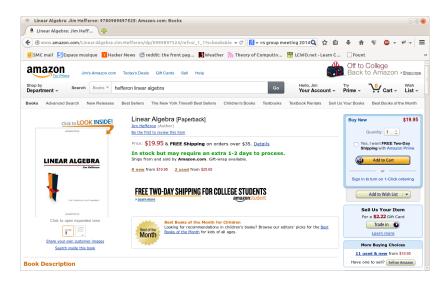
The first chapter finished with a fair understanding of how Gauss's Method solves a linear system. It systematically takes linear combinations of the rows. Here we move to a general study of linear combinations.

We need a setting. At times in the first chapter we've combined vectors from  $\mathbb{R}^2$ , at other times vectors from  $\mathbb{R}^3$ , and at other times vectors from higher-dimensional spaces. So our first impulse might be to work in  $\mathbb{R}^n$ , leaving n unspecified. This would have the advantage that any of the results would hold for  $\mathbb{R}^2$  and for  $\mathbb{R}^3$  and for many other spaces, simultaneously.

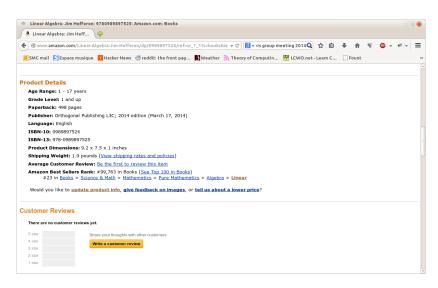
But if having the results apply to many spaces at once is advantageous then sticking only to  $\mathbb{R}^{n/s}$  is overly restrictive. We'd like our results to apply to combinations of row vectors, as in the final section of the first chapter. We've even seen some spaces that are not simply a collection of all of the same-sized column vectors or row vectors. For instance, we've seen a homogeneous system's solution set that is a plane inside of  $\mathbb{R}^3$ . This set is a closed system in that a linear combination of these solutions is also a solution. But it does not contain all of the three-tall column vectors, only some of them.

We want the results about linear combinations to apply anywhere that linear

#### Amazon.com



#### Take that, Mr 99,764



# Felt pretty good

